

# The non-commutative Hardy-Littlewood maximal function on symmetric spaces of $\tau$ -measurable operators

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**Abstract:** In this paper, we investigate the Hardy-Littlewood maximal function on non-commutative symmetric spaces. We complete the results of T. Bekjan and J. Shao. Moreover, we refine the main results of the papers [1] and [2].

**Keywords:** symmetric spaces of functions and operators, Hardy-Littlewood maximal function, von Neumann algebra, (non-commutative) Lorentz and Marcinkiewicz spaces.

**2010 Mathematics Subject Classification:** 46E30, 47B10, 46L51, 46L52, 44A15; Secondary 47L20, 47C15.

## REFERENCES

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