Theoretical study of the Duffing and Van Der Pol oscillators as a stochastic differential equation.

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Abstract: In this work, we will focus on the theoretical study of Duffing and Van Der Pol oscillators, such as the existence, uniqueness and non-explosion of solutions, we start by modeling these two oscillators as, an stochastic differential equation, then based on a non-explosion criterion of Khasminski, we will build Lyapunov functions which ensure the non-explosion of solution, where we will obtain sufficient conditions so that the solution does not explode.

Keywords: Duffing, Van Der Pol, Non-explosion, SDE, Lyaponov Function

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References

- [1] Kazimierz Sobczyk. Stochastic differential equations: with applications to physics and engineering, vol. 40. Springer Science and Business Media, 2013.
- [2] Ioannis Karatzas and Steven Shreve. Brownian motion and stochastic calculus, volume 113. Springer Science and Business Media, 2012.
- [3] Rafail Khasminskii. Stochastic stability of differential equations, volume 66. Springer Science and Business Media, 2011.
- [4] Peter H Baxendale. Stochastic averaging and asymptotic behavior of the stochastic duffing-van der pol equation. Stochastic Processes and Their Applications, 113(2):235-272, 2004.